Studying codimension-2 cycles on surfaces and threefolds via Bloch's higher Chow groups, Hodge theory and deformation theory Herb Clemens

For surfaces, the classical proof of Abel's theorem, applied to quaternionic line bundles associated to Albanese-trivial zero-cycles, gives an answer in Deligne cohomology which may help decide rational equivalence. For families of algebraic one-cycles on certain threefolds, Kuranishi theory applied to Noether-Lefschetz loci makes a plausible case for a variational version of the generalized Hodge conjecture.